

## Cryptography I

### Question 1 *Block Cipher Potpourri*

(20 min)

- (a) Are block ciphers IND-CPA?
- (b) What are good possible sources of entropy for key generation for a block cipher?
- The computer's clock time (assumed in seconds)
  - The Parent Process ID  $\oplus$  my Process ID  $\oplus$  time
  - Hardware noise generator
  - Hardware noise generator  $\oplus$  time
  - 101010101...  $\oplus$  Hardware noise generator
- (c) Why does a block cipher need to be a permutation?

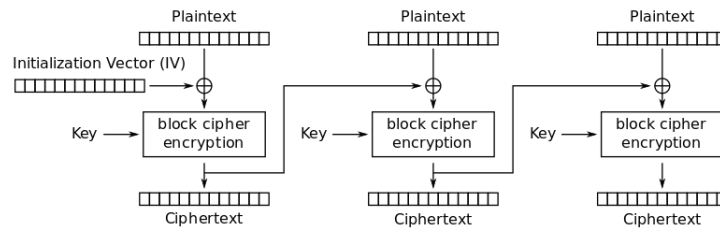
**Question 2** *PRNGs and stream ciphers*

**(20 min)**

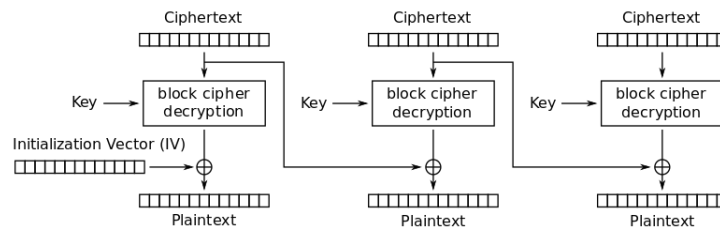
- (a) Pretend I have given you a pseudo-random number generator  $R$ .  $R$  is a function that takes a 128-bit seed  $s$ , an integer  $n$ , and an integer  $m$ , and outputs the  $n^{\text{th}}$  (inclusive) through  $m^{\text{th}}$  (exclusive) pseudo-random bits produced by the generator when it is seeded with seed  $s$ . Use  $R$  to make a secure symmetric-key encryption scheme. That is, define the key generation algorithm, the encryption algorithm, and the decryption algorithm.
- (b) Explain how using a block cipher in counter (CTR) mode is similar to the scenario described above.

**Question 3** *Block cipher security and modes of operation* (20 min)

As a reminder, the cipher-block chaining (CBC) mode of operation works like this:



Cipher Block Chaining (CBC) mode encryption



Cipher Block Chaining (CBC) mode decryption

The output of the encryption is the ciphertext concatenated with the IV that was used.

- (a) Does the initialization vector (IV) have to be non-repeating? Why?
- (b) Imagine you sequentially picked IVs from a list of non-repeating, but publicly-known, numbers, e.g., *A Million Random Digits with 100,000 Normal Deviates* (RAND, 1955).

Say Alice encrypts the one-block long message  $m_1$  with initialization vector  $IV_1$  to get  $C_1$  and encrypts  $m_2$  using  $IV_2$  to get  $C_2$ . She gives these to Mallory and challenges her to tell which  $C$  came from which  $m$ .

Mallory knows that Alice's next IV will be  $IV_3$ , and can ask Alice to encrypt messages for her (a *chosen plaintext attack*). Can Mallory distinguish the two ciphertexts even with this non-repeating IV?